

# Appendix: Mathematical Kernel & Scenario Simulations

## Automation → Local Displacement (Town level)

Equations (key):

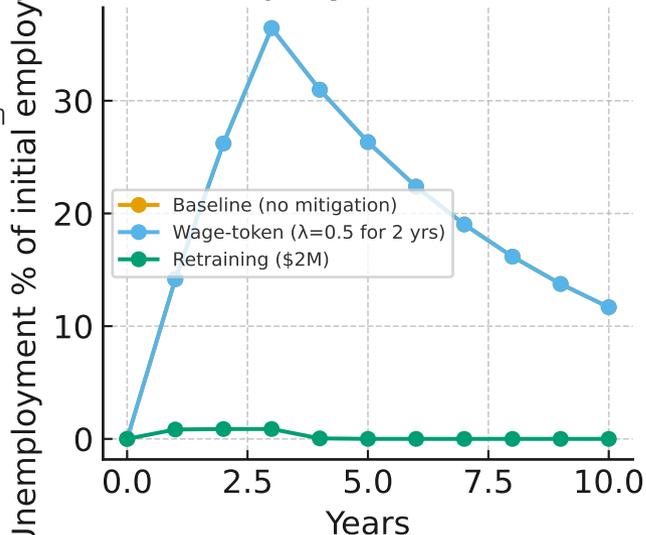
$$1) \Delta Y \approx \kappa \cdot \mu \cdot \Delta W$$

$$2) \Delta L^{\text{avoided}} = \varphi \cdot \Delta K \quad 3) H_t = \eta \cdot U_t$$

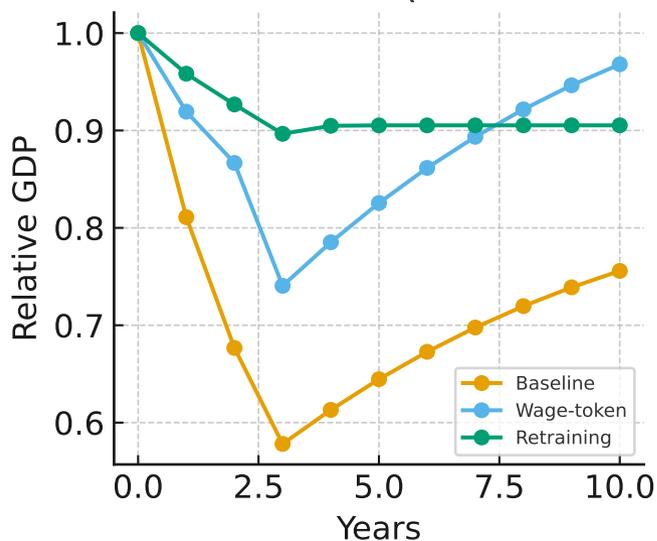
(see text for definitions)

Model snapshot (discrete time, annual): Firm shock → avoided hires:  $\Delta L_t$  Local wage loss:  $\Delta W_t = w \cdot \Delta L_t$   
 Consumption drop:  $\Delta C_t = \mu \cdot \Delta W_t + \mu \cdot S^{\text{token}}_t$   
 Local GDP change:  $\Delta Y_t \approx \kappa \cdot \Delta C_t$  Unemployed pool:  $U_{t+1} = U_t + \Delta L_t - \eta \cdot U_{t+1}$  Re-employment:  $H_t = \eta \cdot U_{t+1}$   
 ·  $U_{t+1}$  (re-employed wage fraction  $\rho$ ) Policy levers:  
 - Wage tokens  $S^{\text{token}}$  (fraction  $\lambda$  of lost wages) - Retraining increases  $\eta$  ( $\eta = \eta_0 + \beta \cdot \text{Spending}$ )

Approx. Unemployment % (simulated)



Local GDP Index (baseline=1.0)



Calibration (selected)  
 Initial local employment L0: 4000  
 Avg annual wage (w): 35000  
 Total avoided hires ( $\Delta L_{\text{total}}$ ) over 3 yrs: 2000  
 Years: 10  
 MPC ( $\mu$ ): 0.5  
 Local multiplier ( $\kappa$ ): 1.3  
 Local tax rate ( $\tau$ ): 0.2  
 Baseline matching rate ( $\eta_0$ ): 0.15  
 Retraining effectiveness ( $\beta$ ) per \$1k: 0.0004  
 Wage-token fraction ( $\lambda$ ) in token scenario: 0.5  
 Profit-share to locals (g): 0.0

Notes: This one-page appendix presents a compact discrete-time kernel. Scenarios: Baseline (no mitigation); Wage-token replaces 50% lost wages for 2 years; Retraining: \$2M one-time program that raises re-employment rate. Parameters should be re-calibrated with local data. See main text for full model.